

b, c

$$m_x \left(-2, -\frac{1}{9} \right)$$

$$f(x) = \frac{x^2 + bx + c}{x^2 - 5x + 4}$$

$$f'(x) = \frac{(2x+b)(x^2-5x+4) - (x^2+bx+c) \cdot (2x-5)}{(x^2-5x+4)^2}$$

$$\begin{cases} -\frac{1}{9} = \frac{4-2b+c}{4+10+4} \end{cases}$$

$$\begin{cases} \frac{6-2b+c}{18} = 0 \end{cases}$$

$$\begin{cases} \frac{6-2b+c}{18} = 0 \end{cases}$$

$$\begin{cases} f'(x) = 0 \\ x = -2 \end{cases}$$

$$\begin{cases} D \left(\frac{x^2+bx+c}{x^2-5x+4} \right) \Big|_{x=-2} = 0 \end{cases}$$

$$\begin{cases} \frac{(-4+b)(18) + (4-2b+c) \cdot (18)}{18^2} = 0 \end{cases}$$

$$\begin{cases} c = 2b - 6 \end{cases}$$

$$\begin{cases} b = \frac{36}{18} = 2 \end{cases}$$

$$\begin{cases} b = 5 \\ c = 4 \end{cases}$$

$$\begin{cases} -72 + 18b + 36 - 18b + 18b - 54 = 0 \end{cases}$$

$$y = \frac{x^2 + 5x + 4}{x^2 - 5x + 4}$$

$$\frac{x^2 + 5x + 4}{x^2 - 5x + 4} \geq 0$$

$$N \geq 0 \Rightarrow x_{1/2} = \frac{-5 \pm \sqrt{25-16}}{2} = \frac{-5 \pm 3}{2} \begin{cases} x_2 = -4 \\ x_2 = -1 \end{cases} \begin{matrix} + & + \\ - & - \end{matrix} \begin{matrix} \uparrow & \downarrow \\ -4 & -1 \end{matrix} S_N: (-\infty; -4] \cup [-1; +\infty)$$

$$D > 0 \Rightarrow x_{1/2} = \frac{5 \pm \sqrt{25-16}}{2} = \begin{cases} x_2 = 4 \\ x_2 = 1 \end{cases} \begin{matrix} + & + \\ - & - \end{matrix} \begin{matrix} \uparrow & \downarrow \\ 1 & 4 \end{matrix} S_D: (-\infty; 1) \cup (4; +\infty)$$

| | | | | | |
|-----|----|----|---|---|---|
| | -4 | -1 | 1 | 4 | x |
| N | + | - | + | - | |
| D | + | + | + | - | |
| N/D | + | - | + | - | |

$f(x) \geq 0$ per $x \leq -4 \cup$
 $\cup -1 \leq x < 1 \cup$
 $\cup x > 4$

finire

$$f'(x) \geq 0$$

