

221 PAG 157

$$f(x) = 3\cos x + 4\sin x$$

$$f(x) = A\cos(x-\alpha) \quad 0 < \alpha < \frac{\pi}{2}$$

• $\operatorname{tg} \alpha = ?$

• grafico $\gamma \in [-\pi, \pi]$

• determina n. soluzioni di $f(x) = 2$ in I

$$y = 3\cos x + 4\sin x \quad a=3 \quad b=4$$

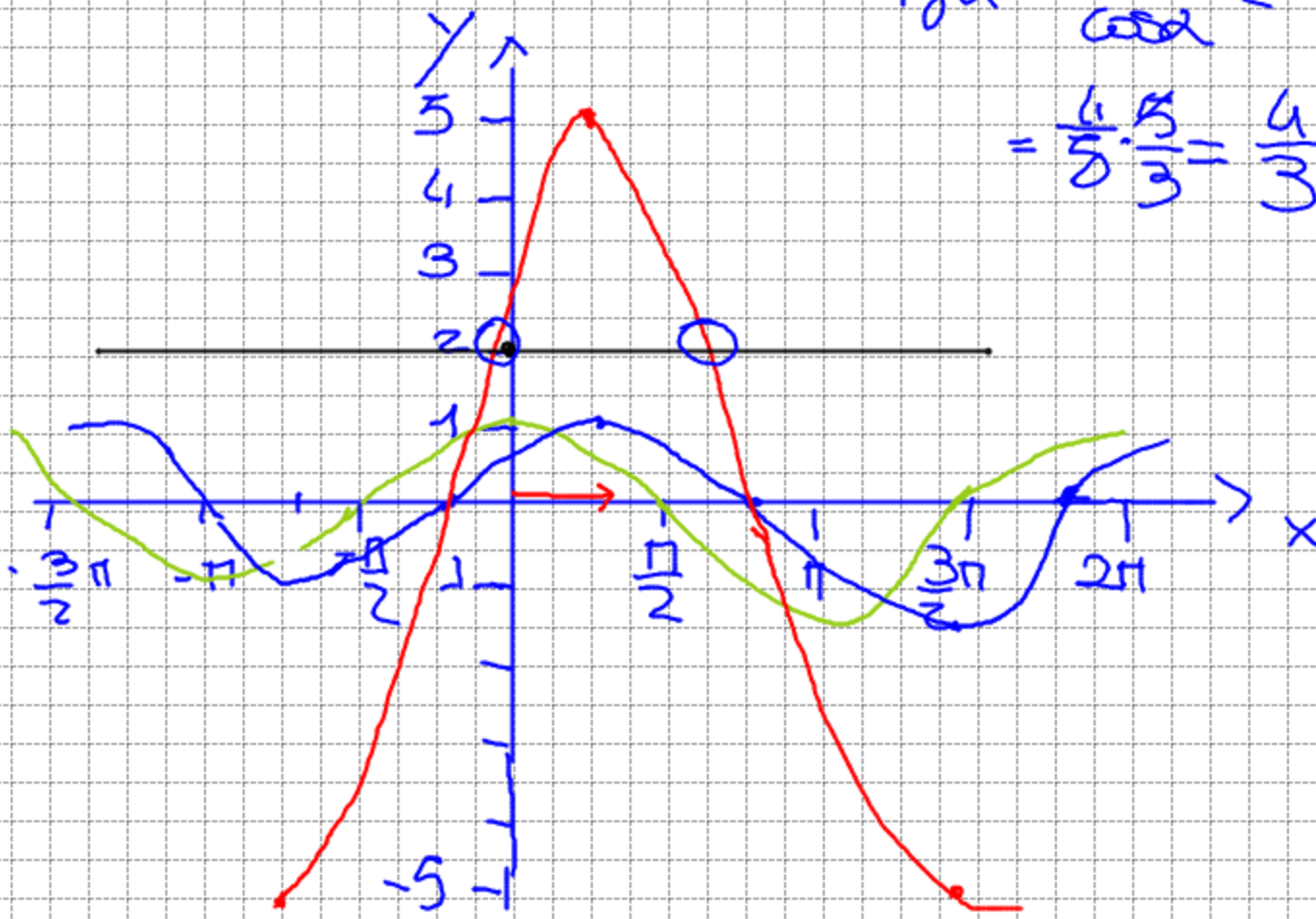
$$\sqrt{a^2+b^2} = \sqrt{9+16} = \sqrt{25} = 5$$

$$y = 5 \left(\frac{3}{5}\cos x + \frac{4}{5}\sin x \right)$$

$$\begin{cases} \cos \alpha = \frac{3}{5} \\ \sin \alpha = \frac{4}{5} \end{cases}$$

$\gamma: y = 5\cos(x-\alpha) \quad \alpha \rightarrow \alpha = 53^\circ 7' 48''$

$$\operatorname{tg} \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{\frac{4}{5}}{\frac{3}{5}} = \frac{4}{3}$$



$$g(x) = \frac{10}{3\cos x + 4\sin x + 7}$$

$D = ? \quad T = ? \quad g(0) = ?$

$$g(x) = \frac{10}{5\cos(x-\alpha) + 7}$$

min = ? max = ?

$D \rightarrow 5\cos(x-\alpha) + 7 \neq 0$

$\cos(x-\alpha) \neq -\frac{7}{5}$

$\cos \alpha = \frac{3}{5}$

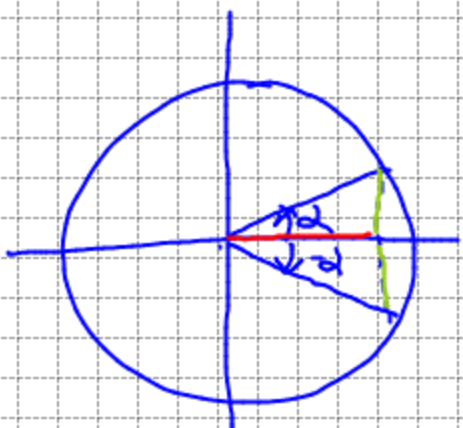
$D = \mathbb{R}$

$T = \frac{2\pi}{1}$

$T = 2\pi$

$$g(0) = \frac{10}{5\cos(-\alpha) + 7}$$

$g(0) = 1$



$5\cos(-\alpha) = 5\cos \alpha$
 $5\sin(-\alpha) = -5\sin \alpha$

MIN = $c - \sqrt{a^2+b^2} = 7 - 5 = 2$

$$g(x) = \frac{10}{5\cos(x-\alpha) + 7}$$

$\alpha = 53^\circ 7' 42''$

$$-1 < \cos(x-2) < 1$$

$$-5 < 5\cos(x-2) < 5$$

$$2 < 5\cos(x-2) + 7 < 12$$

$$\frac{1}{12} < \frac{1}{5\cos(x-2)+7} < \frac{1}{2}$$

$$\frac{5}{6} < \frac{10}{5\cos(x-2)+7} < \frac{10}{2}$$

2/2

$$\frac{1}{2} < \frac{5\cos(x-2)+7}{2}$$

$$\frac{1}{5\cos(x-2)+7} < \frac{5\cos(x-2)+7}{2(5\cos(x-2)+7)}$$

$$\frac{1}{5\cos(x-2)+7} < \frac{1}{2}$$