

ES. N° 11 PAG. 238

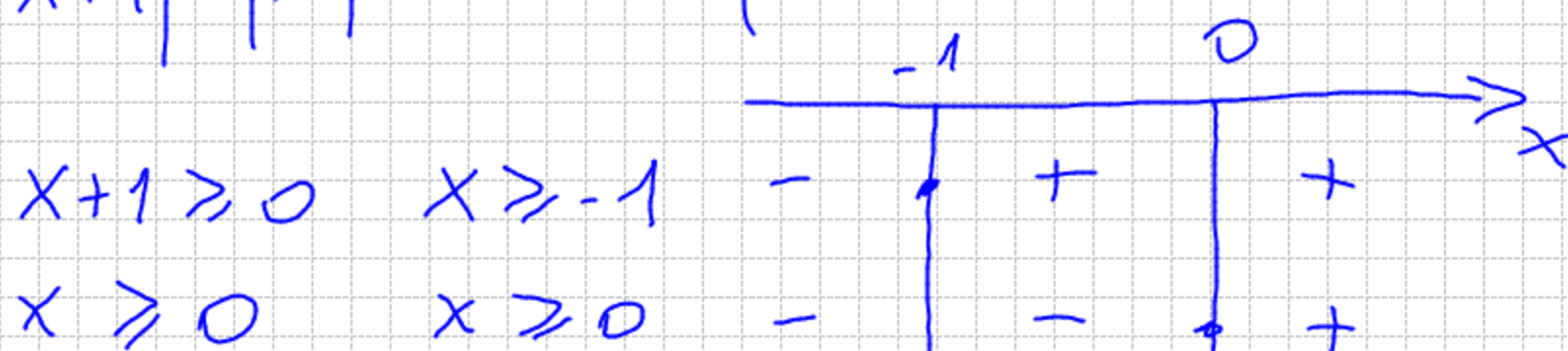
$$f(x) = \frac{2}{x - [x]} \quad \mathcal{D}_f: \left\{ \forall x \in \mathbb{R} / x - [x] \neq 0 \right\} =$$

$$= \mathcal{D}_f: \left\{ \forall x \in \mathbb{R} / x \neq [x] \right\}$$

$$\mathcal{D}_f: \left\{ \forall x \in \mathbb{R} / x \in \mathbb{R} - \mathbb{Z} \right\}$$

ES. N° 13

$$f(x) = \frac{1}{|x+1| - |x|} \quad \mathcal{D}_f: \left\{ \forall x \in \mathbb{R} / |x+1| - |x| \neq 0 \right\} =$$



Se $x < -1$ $f_1(x) = \frac{1}{-x-1+x}$ $f_1(x) = -1$

Se $-1 \leq x < 0$ $f_2(x) = \frac{1}{x+1+x}$ $f_2(x) = \frac{1}{2x+1}$

Se $x \geq 0$ $f_3(x) = \frac{1}{x+1-x}$ $f_3(x) = 1$

$$\mathcal{D}_{f_1} = \left\{ \forall x \in \mathbb{R} / x < -1 \right\} = (-\infty; -1)$$

$$\mathcal{D}_{f_2} = \left\{ \forall x \in \mathbb{R} / \begin{cases} 2x+1 \neq 0 \\ -1 \leq x < 0 \end{cases} \right\} = \left[-1; -\frac{1}{2}\right) \cup \left(-\frac{1}{2}; 0\right)$$

$$\mathcal{D}_{f_3} = \left\{ \forall x \in \mathbb{R} / x \geq 0 \right\} = [0; +\infty)$$

$$f_1(-1) = f_2(-1) = -1$$

$$f_2(0) = f_3(0) = 1$$

$$\mathcal{D}_f = \left(-\infty; -\frac{1}{2}\right) \cup \left(-\frac{1}{2}; +\infty\right)$$

ES. N° 14

$$f(x) = \frac{x^2 + 3x - 2}{x^2 - 2|x| + 1} \quad \mathcal{D}_f: \left\{ x \in \mathbb{R} / x^2 - 2|x| + 1 \neq 0 \right\} =$$



Se $x < 0$ $f_1(x) = \frac{x^2 + 3x - 2}{x^2 + 2x + 1}$ $\mathcal{D}_{f_1}: \left\{ x \in \mathbb{R} / \begin{cases} x < 0 \\ x^2 + 2x + 1 \neq 0 \end{cases} \right\}$

$$\mathcal{D}_{f_1}: \left\{ x \in \mathbb{R} / \begin{cases} x < 0 \\ x \neq -1 \end{cases} \right\} \Rightarrow (-\infty; -1) \cup (-1; 0)$$

Se $x \geq 0$

$$f_2(x) = \frac{x^2 + 3x - 2}{x^2 - 2x + 1}$$

$$D_{f_2} : \left\{ x \in \mathbb{R} / \begin{cases} x \geq 0 \\ x^2 - 2x + 1 \neq 0 \end{cases} \right\} =$$

$$= D_{f_2} : \left\{ x \in \mathbb{R} / \begin{cases} x \geq 0 \\ x \neq 1 \end{cases} \right\} \Rightarrow$$

$$f_1(0) = f_2(0)$$

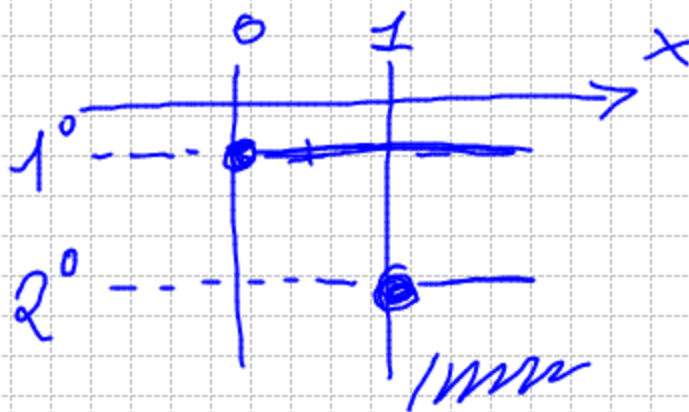
$$D_f = (-\infty; -1) \cup (-1; 1) \cup (1; +\infty) \Rightarrow [0; 1) \cup (1; +\infty)$$

ES. N° 29

$$f(x) = \sqrt{x} + \sqrt{x-1}$$

$$D_f : \left\{ x \in \mathbb{R} / \begin{cases} x \geq 0 \\ x-1 \geq 0 \end{cases} \right\} =$$

$$= D_f : \left\{ x \in \mathbb{R} / \begin{cases} x \geq 0 \\ x \geq 1 \end{cases} \right\} \Rightarrow$$



$$[1; +\infty)$$